

## Sciences and Engineering

Below are examples of questions used for a previous Sciences and Engineering test, so please disregard any references to a lecture.

In the new test, you must answer the compulsory Maths question plus one of the other three questions available.

*Please note, the questions below are for demonstration purposes only and the questions in the final test may take a different format.*

### EXAMPLE COMPULSORY QUESTION

Here we will derive an equation to allow us to use experimental data to evaluate the change in volume ( $\Delta V$ ) when ice melts to form liquid water. Each part carries 4 marks and each part can be done independently from the other parts.

The gradient of the phase boundaries on a phase diagram plotting pressure  $p$  against temperature  $T$  are given by the Clapeyron equation:

$$\frac{dp}{dT} = \frac{H}{T \Delta V} \quad (\text{Eq1})$$

Here  $H$  is the energy change on melting.

(a) Rearrange Eq. (1) and integrate both sides to show:

$$\ln \left( \frac{p_2}{p_1} \right) = \frac{H}{T \Delta V} \quad (\text{Eq2})$$

What are you assuming about  $\Delta V$  and  $H$  in performing this rearrangement?

(b) If the temperature is  $T_1$  when the pressure is  $p_1$  and  $T_2$  when the pressure is  $p_2$  integrate both sides of Eq. 2 to show:

$$T_2 - T_1 = \frac{H}{\Delta V} \ln \left( \frac{p_2}{p_1} \right) \quad (\text{Eq3})$$

(c) Simplify Eq. (3) further, by showing that  $\ln \left( \frac{p_2}{p_1} \right) = \ln \left( 1 + \frac{p_2 - p_1}{p_1} \right)$  and hence:

$$T_2 - T_1 = \frac{H}{\Delta V} \ln \left( 1 + \frac{p_2 - p_1}{p_1} \right) \quad (\text{Eq4})$$

LONDON'S GLOBAL UNIVERSITY  
ARTS AND SCIENCES (BASc)

(d) It can be shown that:

$$(1 + a) \approx (1 + a) + \frac{1}{2} a^2 \quad (\text{Eq5})$$

where  $a = \frac{T_2 - T_1}{T_1}$  and  $a$  is small..

If  $T_2 - T_1$  is small, use Eq. (5) with  $a = (T_2 - T_1)/T_1$  and

